# Analysis of QM Rule Adopted by the EU Inter-Governmental Conference <br> Brussels, 18 June 2004 

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#### Abstract

We analyse and evaluate the qualified majority (QM) decision rule for the Council of Ministers of the EU adopted at the EU Inter-Governmental Conference, Brussels, 18 June 2004 [1]. We compare this rule with the QM rule prescribed in the Treaty of Nice, and the rule included in the original draft Constitution proposed by the European Convention in July 2003. We use a method similar to the one we used in [3] and [4].


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## 1 Introductory remarks

The agreement reached at the Brussels IGC, 17-18 June 2004, amends the QM rule in the draft Constitution as follows:

Article I-24

1. A qualified majority shall be defined as at least $55 \%$ of the members of the Council, comprising at least fifteen of them and representing Member States comprising at least $65 \%$ of the population of the Union.
A blocking minority must include at least four Council members, failing which the qualified majority shall be deemed attained.
2. By derogation from paragraph 1 , when the Council is not acting on a proposal from the Commission or from the Union Minister for Foreign Affairs, the qualified majority shall be defined as $\mathbf{7 2 \%}$ of the members of the Council, representing Member States comprising at least $\mathbf{6 5 \%}$ of the population of the Union. ${ }^{1}$

We shall not deal with the last paragraph (2), which applies in certain exceptional circumstances.

Also, we shall only deal with the effect of the new QM rule in the scenario of a 27 -member EU. This is because the provisions of the Treaty of Nice will continue to apply until 31 October 2009, ${ }^{2}$ by which time the EU will almost certainly have been enlarged to include (at least) Romania and Bulgaria.

Using the latest population figures available to us, ${ }^{3}$ we find that the clause excluding blocking coalitions with less than four members rules out (under the 27 -member scenario) just the following ten coalitions, whose populations comprise more than $35 \%$ of the total, and therefore would otherwise be able to block.

[^0]1. Germany, France, UK;
2. Germany, France, Italy;
3. Germany, France, Spain;
4. Germany, France, Poland;
5. Germany, UK, Italy;
6. Germany, UK, Spain;
7. Germany, UK, Poland;
8. Germany, Italy, Spain;
9. Germany, Italy, Poland;
10. France, UK, Italy.

Accordingly, the complementary ten 24 -member coalitions will be winning coalitions, although their populations comprise less than $65 \%$ of the total.

The structure of the tables in this paper is the same as in our [4], to which the reader is referred for explanations.

We denote by $\mathcal{D}_{27}, \mathcal{N}^{\prime}{ }_{27}$ and $\mathcal{C}_{27}$, respectively, the new QM rule, the rule prescribed by the Nice Treaty, and the rule included in the original draft Constitution (all under the 27 -member scenario). Rule B is our benchmark rule, with voting powers very nearly proportional to population square roots, and quota set at $60 \%$ of the total weight.

## 2 Conclusions

From Table 5 we can see that $\mathcal{D}_{27}$ is quite inequitable by the yardstick of Penrose's Square-Root Rule. Its overall distortion, as measured by the distortion index $D$, is not quite so bad as that of the original version $\mathcal{C}_{27}$ proposed in the draft Constitution. However, its 'local' distortions - the individual deviations from equitability - are more extreme than those of $\mathcal{C}_{27}$. From the last column of Table 2 we can see that the two most egregious cases are: on the one hand Malta, which has $138.5 \%$ more than its fair share; and on the other hand Greece, which has $17.4 \%$ too little.

In [4] we saw that $\mathcal{C}_{27}$ was biased in favour of the four largest and six smallest member-states. Table 2 now shows that the same is true of $\mathcal{D}_{27}$, but
now the bias in favour of the six smallest member-states is more pronounced, whereas that in favour of the four biggest is less so.

Returning to Table 5, we observe that $\mathcal{D}_{27}$ is quite effective: it has a relatively high value of Coleman's index $A$ (the a priori probability of approving an act rather than blocking it) and a correspondingly low resistance R. In betting terms, this means that the a priori odds against approval of an act are approximately 27 to 4 (whereas under $\mathcal{C}_{27}$ they would be approximately 25 to 7 ). The values of these parameters are not very different from what they were in the periods 1973-80 and 1980-85, when the EU had nine or ten members. In our view they are very reasonable.

With respect to $A$ and R , as well as with respect to sensitivity S and mean majority deficit (MMD), $\mathcal{D}_{27}$ is intermediate between $\mathcal{N}^{\prime}{ }_{27}$ and $\mathcal{C}_{27}$.

Table 3 compares $\mathcal{D}_{27}$ with $\mathcal{N}^{\prime}{ }_{27}$. We see that $\mathcal{D}_{27}$ gives all member-states more absolute voting power (as measured by $\psi$ ), but the increase is very uneven, not to say erratic. In [4] we saw that $\mathcal{C}_{27}$ would improve the relative positions (measured by $\beta$ ) of the four largest and six smallest member-states compared to their positions under $\mathcal{N}^{\prime}{ }_{27}$. We now see that $\mathcal{D}_{27}$ does the same; but unlike $\mathcal{C}_{27}$ it also improves the relative positions of two other members: Denmark and Slovakia. As for blocking power, $\gamma$, Malta is the only gainer in comparison with $\mathcal{N}^{\prime}{ }_{27}$; all other member-states lose blocking power, but the extent of loss is again very uneven.

Table 4 compares $\mathcal{D}_{27}$ with $\mathcal{C}_{27}$. We see that $\mathcal{D}_{27}$ gives all member-states less absolute voting power and greater blocking power than $\mathcal{C}_{27}$ would have done. But in relative terms the six largest member-states - from Germany down to Poland - do slightly less well under $\mathcal{D}_{27}$, whereas all the others do slightly better.

## 3 Tables

Table 1: Population of 27 present and prospective EU members

| Country | Population | Pop.\% | Pop. sqrt. | Pop. sqrt. $\%$ |
| :--- | ---: | ---: | ---: | ---: |
| Germany | $82,536,700$ | 17.047 | $9,084.97$ | 9.54 |
| France | $59,630,100$ | 12.316 | $7,722.05$ | 8.11 |
| UK | $59,328,900$ | 12.254 | $7,702.53$ | 8.09 |
| Italy | $57,321,000$ | 11.839 | $7,571.06$ | 7.95 |
| Spain | $41,550,600$ | 8.582 | $6,445.98$ | 6.77 |
| Poland | $38,218,500$ | 7.894 | $6,182.11$ | 6.49 |
| Romania | $21,772,800$ | 4.497 | $4,666.13$ | 4.90 |
| Netherlands | $16,192,600$ | 3.344 | $4,024.00$ | 4.23 |
| Greece | $11,018,400$ | 2.276 | $3,319.40$ | 3.49 |
| Portugal | $10,407,500$ | 2.150 | $3,226.07$ | 3.39 |
| Belgium | $10,355,800$ | 2.139 | $3,218.04$ | 3.38 |
| Czech Rep | $10,203,300$ | 2.107 | $3,194.26$ | 3.36 |
| Hungary | $10,142,400$ | 2.095 | $3,184.71$ | 3.35 |
| Sweden | $8,940,800$ | 1.847 | $2,990.12$ | 3.14 |
| Austria | $8,067,300$ | 1.666 | $2,840.30$ | 2.98 |
| Bulgaria | $7,845,800$ | 1.621 | $2,801.04$ | 2.94 |
| Denmark | $5,383,500$ | 1.112 | $2,320.24$ | 2.44 |
| Slovakia | $5,379,200$ | 1.111 | $2,319.31$ | 2.44 |
| Finland | $5,206,300$ | 1.075 | $2,281.73$ | 2.40 |
| Ireland | $3,963,600$ | 0.819 | $1,990.88$ | 2.09 |
| Lithuania | $3,462,600$ | 0.715 | $1,860.81$ | 1.95 |
| Latvia | $2,331,500$ | 0.482 | $1,526.93$ | 1.60 |
| Slovenia | $1,995,000$ | 0.412 | $1,412.45$ | 1.48 |
| Estonia | $1,356,000$ | 0.280 | $1,164.47$ | 1.22 |
| Cyprus | 715,100 | 0.148 | 845.64 | 0.89 |
| Luxembourg | 448,300 | 0.093 | 669.55 | 0.70 |
| Malta | 397,300 | 0.082 | 630.32 | 0.66 |
| Total | $484,170,900$ | 100.003 | 95195.10 | 99.98 |

Note Source of population figures: [2]. The apparent discrepancies in the totals of the second and last columns are due to rounding errors.

Table 2: QM rule $\mathcal{D}_{27}$

| Country | w | $\psi$ | $100 \beta$ | $\gamma$ | Quotient |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Germany | 1705 | 0.204161 | 11.8702 | 0.79273 | 1.244 |
| France | 1232 | 0.150306 | 8.7389 | 0.58362 | 1.077 |
| UK | 1225 | 0.149536 | 8.6942 | 0.58063 | 1.075 |
| Italy | 1184 | 0.145129 | 8.4380 | 0.56352 | 1.061 |
| Spain | 858 | 0.109655 | 6.3755 | 0.42578 | 0.942 |
| Poland | 789 | 0.101270 | 5.8880 | 0.39322 | 0.907 |
| Romania | 450 | 0.072553 | 4.2183 | 0.28171 | 0.861 |
| Netherlands | 334 | 0.060284 | 3.5050 | 0.23408 | 0.829 |
| Greece | 228 | 0.049531 | 2.8798 | 0.19232 | 0.826 |
| Portugal | 215 | 0.048213 | 2.8031 | 0.18720 | 0.827 |
| Belgium | 214 | 0.048109 | 2.7971 | 0.18680 | 0.827 |
| Czech Rep | 211 | 0.047807 | 2.7796 | 0.18563 | 0.828 |
| Hungary | 209 | 0.047603 | 2.7677 | 0.18484 | 0.827 |
| Sweden | 185 | 0.045175 | 2.6265 | 0.17541 | 0.836 |
| Austria | 167 | 0.043349 | 2.5203 | 0.16832 | 0.845 |
| Bulgaria | 162 | 0.042843 | 2.4910 | 0.16636 | 0.847 |
| Denmark | 111 | 0.037670 | 2.1902 | 0.14627 | 0.899 |
| Slovakia | 111 | 0.037670 | 2.1902 | 0.14627 | 0.899 |
| Finland | 108 | 0.037363 | 2.1723 | 0.14508 | 0.906 |
| Ireland | 82 | 0.034726 | 2.0190 | 0.13484 | 0.965 |
| Lithuania | 72 | 0.033704 | 1.9596 | 0.13087 | 1.002 |
| Latvia | 48 | 0.031254 | 1.8172 | 0.12136 | 1.133 |
| Slovenia | 41 | 0.030535 | 1.7753 | 0.11856 | 1.197 |
| Estonia | 28 | 0.029212 | 1.6984 | 0.11343 | 1.388 |
| Cyprus | 15 | 0.027878 | 1.6209 | 0.10825 | 1.825 |
| Luxembourg | 9 | 0.027259 | 1.5849 | 0.10585 | 2.253 |
| Malta | 8 | 0.027158 | 1.5790 | 0.10545 | 2.385 |
| Total | 10001 | 1.719953 | 100.0002 |  |  |

Table 3: QM rule $\mathcal{D}_{27}$ compared to $\mathcal{N}^{\prime}{ }_{27}$

| Country | $\psi\left[\mathcal{D}_{27}\right] / \psi\left[\mathcal{N}^{\prime}{ }_{27}\right]$ | $\beta\left[\mathcal{D}_{27}\right] / \beta\left[\mathcal{N}^{\prime}{ }_{27}\right]$ | $\gamma\left[\mathcal{D}_{27}\right] / \gamma\left[\mathcal{N}^{\prime}{ }_{27}\right]$ |
| :--- | ---: | ---: | ---: |
| Germany | 6.245729 | 1.5257 | 0.98249 |
| France | 4.598195 | 1.1233 | 0.72332 |
| UK | 4.574655 | 1.1175 | 0.71962 |
| Italy | 4.439859 | 1.0846 | 0.69841 |
| Spain | 3.518676 | 0.8596 | 0.55351 |
| Poland | 3.249634 | 0.7938 | 0.51118 |
| Romania | 4.055848 | 0.9908 | 0.63801 |
| Netherlands | 3.611800 | 0.8823 | 0.56815 |
| Greece | 3.200845 | 0.7819 | 0.50351 |
| Portugal | 3.115648 | 0.7611 | 0.49011 |
| Belgium | 3.108956 | 0.7595 | 0.48905 |
| Czech Rep | 3.089425 | 0.7547 | 0.48598 |
| Hungary | 3.076248 | 0.7515 | 0.48391 |
| Sweden | 3.478080 | 0.8496 | 0.54712 |
| Austria | 3.337459 | 0.8153 | 0.52500 |
| Bulgaria | 3.298542 | 0.8058 | 0.51888 |
| Denmark | 4.099205 | 1.0014 | 0.64483 |
| Slovakia | 4.099205 | 1.0014 | 0.64483 |
| Finland | 4.065775 | 0.9932 | 0.63957 |
| Ireland | 3.778841 | 0.9231 | 0.59443 |
| Lithuania | 3.667634 | 0.8960 | 0.57694 |
| Latvia | 5.952199 | 1.4540 | 0.93631 |
| Slovenia | 5.815234 | 1.4206 | 0.91477 |
| Estonia | 5.563331 | 1.3590 | 0.87514 |
| Cyprus | 5.309266 | 1.2970 | 0.83517 |
| Luxembourg | 5.191457 | 1.2682 | 0.81664 |
| Malta | 6.859621 | 1.6757 | 1.07905 |

Table 4: QM rule $\mathcal{D}_{27}$ compared to $\mathcal{C}_{27}$

| Country | $\psi\left[\mathcal{D}_{27}\right] / \psi\left[\mathcal{C}_{27}\right]$ | $\beta\left[\mathcal{D}_{27}\right] / \beta\left[\mathcal{C}_{27}\right]$ | $\gamma\left[\mathcal{D}_{27}\right] / \gamma\left[\mathcal{C}_{27}\right]$ |
| :--- | ---: | ---: | ---: |
| Germany | 0.676013 | 0.9276 | 1.14929 |
| France | 0.698817 | 0.9589 | 1.18805 |
| UK | 0.700510 | 0.9613 | 1.19093 |
| Italy | 0.700751 | 0.9616 | 1.19134 |
| Spain | 0.709691 | 0.9739 | 1.20654 |
| Poland | 0.680431 | 0.9337 | 1.15680 |
| Romania | 0.754626 | 1.0355 | 1.28294 |
| Netherlands | 0.751772 | 1.0316 | 1.27808 |
| Greece | 0.759113 | 1.0417 | 1.29056 |
| Portugal | 0.759286 | 1.0419 | 1.29086 |
| Belgium | 0.757655 | 1.0397 | 1.28808 |
| Czech Rep | 0.760008 | 1.0429 | 1.29209 |
| Hungary | 0.756767 | 1.0385 | 1.28657 |
| Sweden | 0.764274 | 1.0488 | 1.29934 |
| Austria | 0.763640 | 1.0479 | 1.29826 |
| Bulgaria | 0.766646 | 1.0520 | 1.30337 |
| Denmark | 0.771315 | 1.0584 | 1.31131 |
| Slovakia | 0.771315 | 1.0584 | 1.31131 |
| Finland | 0.774320 | 1.0625 | 1.31642 |
| Ireland | 0.776491 | 1.0655 | 1.32011 |
| Lithuania | 0.779308 | 1.0694 | 1.32490 |
| Latvia | 0.787012 | 1.0800 | 1.33799 |
| Slovenia | 0.786396 | 1.0791 | 1.33695 |
| Estonia | 0.788179 | 1.0816 | 1.33998 |
| Cyprus | 0.790007 | 1.0841 | 1.34309 |
| Luxembourg | 0.799177 | 1.0967 | 1.35868 |
| Malta | 0.796190 | 1.0926 | 1.35360 |

Table 5: Synoptic comparison

| Rule | $D$ | $\max \|d\|$ | $\operatorname{ran}(d)$ | MMD | S | $A$ | R |
| :--- | :---: | ---: | ---: | ---: | :---: | :---: | :---: |
| Pre-Nice | 5.1903 | 124.1 | 144.2 | 5519 | 0.861 | 0.078 | 0.844 |
| $\mathcal{C}_{27}$ | 8.7090 | 118.2 | 139.0 | 3761 | 0.965 | 0.219 | 0.562 |
| $\mathcal{N}^{\prime}{ }_{27}$ | 4.8227 | 77.6 | 99.7 | 7937 | 0.858 | 0.020 | 0.959 |
| $\mathcal{D}_{27}$ | 7.5574 | 138.5 | 155.9 | 5223 | 0.945 | 0.129 | 0.742 |
| Rule B | 0.2490 | 1.2 | 2.1 | 3882 | 0.966 | 0.198 | 0.605 |

$D, \max |d|$ and $\operatorname{ran}(d)$ are given in percentages.

## References

[1] Conference of the Representatives of the Governments of the Member States, Brussels, 18 June 2004. EU document CIG 85/04
[2] EUROSTAT (the statistical office of the European Commission):
http://europa.eu.int/comm/eurostat/.
[3] Felsenthal D S and Machover M 2001: 'The Treaty of Nice and qualified majority voting, Social Choice and Welfare 18:431-464. Downloadable from
http://www.lse.ac.uk/Depts/cpnss/projects/vp.html
[4] - 2004: 'Analysis of QM rules in the draft Constitution for Europe proposed by the European Convention, 2003'. Forthcoming in Social Choice and Welfare 23:1-20. Downloadable from http://www.lse.ac.uk/Depts/cpnss/projects/vp.html


[^0]:    ${ }^{1}$ See [1, p. 7].
    ${ }^{2}$ See [1, p. 8].
    ${ }^{3}$ Taken from Eurostat [2].

